

## Revision 'Must Know' Checklist: Y9 Maths Higher Tier (Upper)

Below is a checklist of everything you must know to be successful by the end of this year.



Number	Algebra	Geometry and Measures	Ratio and Proportion	Statistics and Probability
<ul style="list-style-type: none"> <li>Use product rule for counting and finding potential combinations</li> <li>Use BIDMAS to complete complex calculations</li> <li>Solve estimation problems to one and two-step calculations</li> <li>Evaluate positive numerical indices (not algebraic)</li> <li>Solve numerical indices equations with different base numbers and missing powers. EG <math>8^3 = 2^?</math></li> <li>Evaluate algebraic positive numerical indices.</li> <li>Evaluate more complex problems such as <math>25^{1.5}</math></li> <li>Find the HCF of 2 numbers using either lists of common factors or a Venn diagram</li> <li>Solve worded HCF and LCM problems using product of Primes</li> <li>Convert large numbers into and out of standard form</li> <li>Convert small numbers into and out of standard form</li> <li>Add and subtract numbers in standard form</li> <li>Multiply and divide numbers in standard form</li> </ul>	<ul style="list-style-type: none"> <li>Substitute positive and negative numbers into expressions without a calculator</li> <li>Expand single brackets (Recap) and double brackets and simplify expressions</li> <li>Solve linear equations, with integer coefficients, in which the unknown appears on either side or on both sides of the equation</li> <li>Change the subject of a formula (one and two-step)</li> <li>Change the subject of a formula involving powers and roots</li> <li>Factorise quadratic expressions in the form <math>ax^2 + bx + c</math> where <math>a=2</math></li> <li>Solve quadratic equations by factorising in the form <math>ax^2 + bx + c = 0</math> where <math>a=1</math></li> <li>Factorise quadratic expressions in the form <math>ax^2 + bx + c</math> where <math>a&gt;1</math></li> <li>Draw linear graphs such as <math>x=4</math>, <math>y=-1</math></li> <li>Draw linear graphs in the form <math>y=mx+c</math> from a table of values</li> <li>Draw linear graphs such as <math>y = mx</math></li> <li>Identify the gradient of a straight line from a graph</li> </ul>	<ul style="list-style-type: none"> <li>Understand and use the angle properties of parallel lines and find missing angles using the properties of corresponding and alternate angles giving reasons, include geometric shapes and their properties</li> <li>Understand, recall and use Pythagoras' Theorem in 2D. Given three sides of a triangle, justify if it is right-angled or not</li> <li>Give an answer to the use of Pythagoras' Theorem in surd form</li> <li>Understand, recall and use Pythagoras' Theorem in 2D. Given three sides of a triangle, justify if it is right-angled or not</li> <li>Find the interior angle of a polygon</li> <li>Calculate the angles of regular polygons and use these to solve geometric problems</li> <li>Find the exterior angle of a polygon</li> <li>Find the number of sides of a polygon give the interior or exterior angle</li> <li>Solve exam style questions on angle problems</li> <li>Calculate the length of the hypotenuse and a shorter side in</li> </ul>	<ul style="list-style-type: none"> <li>Solve problems involving Pressure, Area, Force, include changes of units</li> <li>Solve problems involving Density, Mass, Volume, include changes of units</li> <li>Solve problems involving Speed, Distance, Time. miles per hour as well as metric measures, include changes of units.</li> <li>Convert between units of compound measures.</li> <li>Metric speed measures, density measures and pressure measures</li> <li>Calculate an unknown quantity from quantities that vary in direct or inverse proportion</li> <li>Recognise when values are in direct proportion by reference to the graph form, and use a graph to find the value of <math>k</math> in <math>y = kx</math>.</li> <li>Identify direct proportion from a table of values, by comparing ratios of values, for <math>x</math> squared and <math>x</math> cubed relationships.</li> <li>Relate algebraic solutions to graphical representation of the equations</li> <li>Solve problems involving direct proportion or inverse proportion with squares, cubes or other</li> </ul>	<ul style="list-style-type: none"> <li>Sort, classify and tabulate data and discrete or continuous quantitative data</li> <li>Find averages and measures of spread from lists of numbers</li> <li>Recognise advantages and disadvantages of between measures of average</li> <li>Compare the mean and range of two distributions, or median or mode as appropriate</li> <li>Produce and interpret composite and dual bar charts.</li> <li>Produce and interpret pie charts.</li> <li>Find the mode and the frequency represented by each sector.</li> <li>Describe the advantages and limitations of pie charts</li> <li>Calculate the mean, mode, median and range from a frequency table (discrete data).</li> <li>Compare data sets using averages and range</li> <li>Find the mean from a grouped frequency table</li> <li>Construct and interpret an ordered stem and leaf diagram</li> </ul>

<ul style="list-style-type: none"> <li>Identify Surds and simplify</li> <li>Rationalize Surds - Single Surd denominator</li> <li>Use Surds in complex operations</li> <li>Rationalize Surds including complex double brackets, i.e. <math>3 + \sqrt{2}</math></li> <li>Solve problems using the order of operations (BIDMAS)</li> <li>Order Fractions, Decimals and Percentages</li> <li>Add and subtract proper, improper fractions and mixed numbers</li> <li>Multiply and divide proper, improper fractions and mixed numbers</li> <li>Convert a recurring decimal into a fraction</li> <li>Find a percentage of an amount</li> <li>Find percentage increases &amp; decreases using both non-calculator and calculator methods</li> <li>Solve worded percentage increase and decrease problems</li> <li>Solve percentage change problems</li> <li>Solve reverse/backward percentage problems</li> </ul>	<ul style="list-style-type: none"> <li>Identify the gradient and y-intercept from a graph</li> <li>Find the equation of a positive straight line given two points</li> <li>Find the equation of a positive straight line and given the gradient and a point</li> <li>Plot a straight line graph given the gradient and y-intercept</li> <li>Calculate the length of a line segment given the coordinates of the end points – Pythagoras</li> <li>Use straight line graphs to solve currency conversion graphs</li> <li>Solve currency conversion problems by extrapolating</li> <li>Draw and interpret straight-line graphs for real-life situations, including ready reckoner graphs, conversion graphs, fuel bills, fixed charge and cost per item (gradient)</li> <li>Draw a distance–time graph and Use to calculate various measures (of individual sections), including average speed, distance, time</li> <li>Generate points and plot graphs of simple quadratic functions, then more general quadratic functions. Find approximate solutions. Why is it an approximate?</li> <li>Solve linear equations with unknowns on one (Recap) and</li> </ul>	<ul style="list-style-type: none"> <li>a right-angled triangle problems (including decimal lengths and a range of units).</li> <li>Find the area and perimeter of composite shapes made up of rectangles, triangles, parallelograms and trapeziums</li> <li>Discover the pi as a ratio and describe its significance</li> <li>Use pi to find the circumference of a circle (with and without calculator)</li> <li>Find the area circumference of a circle</li> <li>Find the area of semi circles / quarter of circles</li> <li>Find the area and perimeter of a sector of a circle including arcs</li> <li>Find the surface area of prisms including cubes, cuboids, and triangular prisms</li> <li>Find the volume of prisms including cubes, cuboids, and triangular prisms</li> <li>Find the surface area and volume of a cylinder</li> <li>Convert between metric measures of volume and capacity, e.g. <math>1 \text{ ml} = 1 \text{ cm}^3</math></li> <li>Calculate the upper and lowers bounds of numbers given to varying degrees of accuracy,</li> </ul>	<ul style="list-style-type: none"> <li>powers/roots of another quantity, include using k to find another value.</li> <li>Understand and use SSS, SAS, ASA and RHS conditions to prove the congruence of triangles using formal arguments, and to verify standard ruler and pair of compasses constructions.</li> <li>Share within a given 2 part ratio</li> <li>Solve recipe problems</li> <li>Solve worded ratio problems by upscaling and downscaling</li> <li>Solve challenging problems using ratio (i.e. combining ratio with factor problems from past papers)</li> </ul>	<ul style="list-style-type: none"> <li>Construct a back-to-back stem and leaf diagram and interpret it</li> <li>Find the mode, median, range, as well as the greatest and least values from stem and leaf diagrams, and compare two distributions from stem and leaf diagrams</li> <li>Construct a frequency polygon</li> <li>Draw and interpret Scattergraphs</li> <li>Describe a Scattergraphs correlation</li> <li>Draw a line of best fit</li> <li>Differentiate between experimental versus theoretical probability</li> <li>Create a sample space diagram for experiments</li> <li>Find probability from two-way tables</li> <li>Find probabilities using Frequency Trees</li> <li>Solve independent probability problems using probability trees</li> <li>Solve conditional probability problems using probability trees</li> <li>Shade areas of a Venn diagram and use correct notation TBAT fill in a Venn diagram correctly given two sets of data</li> </ul>
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<ul style="list-style-type: none"> <li>• Solve simple interest problems</li> <li>• Solve compound interest problems inc. Depreciation</li> <li>• Write ratios in their simplest form, including three part ratios.</li> <li>• Divide into a given ratio with two or more parts</li> <li>• Write a ratio as a linear function</li> </ul>	<p>both sides with positive, negative and fractional answers</p> <ul style="list-style-type: none"> <li>• Solve double inequalities and represent on a number line.</li> <li>• Change the subject of a formula (multi-step)</li> <li>• Solve linear simultaneous equations using elimination where co-efficients are the same and answers positive</li> <li>• Solve simultaneous equations graphically</li> <li>• Solve double inequalities and represent on a number line.</li> <li>• Find the solution sets and compare them to see which value of <math>x</math> satisfies both solve linear inequalities in two variables algebraically</li> <li>• Factorise quadratic expressions in the form <math>ax^2 + bx + c</math>.</li> <li>• Solve quadratic equations by factorising, including ones that need rearranging</li> <li>• Solve quadratic equations by using the quadratic formula</li> <li>• Write a quadratic in completing the square form.</li> <li>• Use to solve quadratic equations</li> <li>• Expand the product of more than two linear expressions, triple brackets.</li> </ul>	<p>include whole numbers, decimal places and significant figures.</p> <ul style="list-style-type: none"> <li>• Find the upper and lower bounds of calculations involving perimeters, areas and volumes of 2D and 3D shapes</li> <li>• Use inequality notation to specify an error interval due to truncation or rounding</li> <li>• Reflect a 2D shape in a line such as <math>x=4</math> or <math>y=-1</math> and be able to describe the transformation</li> <li>• Reflect a 2D shape in the line <math>y=x</math> and/ or <math>y=-x</math> and be able to describe the transformation</li> <li>• Translate a 2D shape using a vector</li> <li>• Describe a translation of a 2D shape using a vector</li> <li>• Rotate a 2D shape on a set of axis</li> <li>• Describe a rotation of a 2D shape on a set of axis</li> <li>• Enlarge a 2D shape on a set of axis using a positive, negative and fractional scale factor using vectors</li> <li>• Describe a transformation is a rotation, translation, enlargement or reflection as exam style questions</li> <li>• Understand and draw front and side elevations and plans of shapes made from simple solids</li> </ul>	<ul style="list-style-type: none"> <li>• Find probability from Venn diagram with two sets of data</li> <li>• Work out probabilities from Venn diagrams to represent real-life situations and also 'abstract' sets of numbers/values, such as sets of prime and even number</li> <li>• Compare experimental data and theoretical probabilities., include samples of different sizes.</li> <li>• Estimate the number of times an event will occur, given the probability and the number of trials</li> <li>• Plot a scatter graph and draw accurately a line of best fit</li> <li>• Use a line of best fit to solve scatter graph problems</li> <li>• Draw a pie chart</li> <li>• Compare and interpret pie chart questions</li> <li>• Draw a cumulative frequency diagram</li> <li>• Find averages and measures of spread from a cumulative frequency graph i.e Median and IQR</li> <li>• Compare distributions using cumulative frequency diagrams</li> <li>• Draw a boxplot/ Box and Whisker diagram from a discrete set of numbers</li> </ul>
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